

Effect of plasma actuation on asymmetric vortex flow over a slender conical forebody

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The active flow control technology by using plasma actuation to manipulate forebody vortices on a slender conical body is being studied based on the previous research. This work is motivated by the need to increase the experimental velocity in the wind tunnel via an effective streamlining created by the actuators. A pair of Single-Dielectric Barrier Discharge (SDBD) plasma actuators is installed near the tip of a 20° circular-cone-cylinder model. The experiments are performed in a 3.0 m×1.6 m low speed wind tunnel at angles of attack of 45° and 50°. The test wind speed is varied from 15 m/s to 30 m/s with Reynolds numbers ranging from 0.16 to 0.32 million based on the cone base diameter. The results consist of measurements of circumferential pressure distributions over nine stations along the cone forebody, including one station using unsteady pressure tappings. The cross-sectional and overall side forces and yawing moments over the cone are calculated from the measured pressures. The experiments have confirmed that the plasma actuator can be used to achieve the proportional lateral control on slender forebodies at high angles of attack combined with a duty cycle technique. An effective control with a relative higher wind speed can be gotten by adjusting the position and induced flow direction of the plasma actuators.

Nomenclature

C_n	= yawing moment coefficient about cone base, yawing moment/ $q_\infty SD$
C_p	= pressure coefficient
C_Y	= overall side-force coefficient, overall side force/ $q_\infty S$
C_{Yd}	= time-averaged local side-force coefficient, local side force/ $q_\infty d$
D	= base diameter of circular cone forebody
d	= local diameter of circular cone forebody
F	= frequency of AC voltage source
f^+	= reduced frequency of actuator, fD/U_∞
f	= frequency of duty cycle
L	= length of circular cone forebody
M	= mach number
q_∞	= free-stream dynamic pressure
Re	= free-stream Reynolds number based on D , $U_\infty D/\nu$
S	= base area of circular cone forebody
T	= period of duty cycle

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t	= time of duty cycle
U_∞	= free-stream velocity
V_{p-p}	= amplitude of oscillation
x, y, z	= body coordinates, x toward base, y toward starboard, right-hand system
α	= angle of attack
θ	= meridian angle measured from windward generator, positive when clockwise
τ	= fraction of time when starboard actuator is on over a duty-cycle period
ν	= coefficient of kinematic viscosity

I. Introduction

The demand for greater maneuverability requires fighter flight through large angles of attack. For many modern fighter aircraft, the nose portion of the fuselage consists of a long slender pointed forebody, over which the initially symmetric separation vortices become asymmetric as the angle of attack is increased beyond a certain value, causing large lateral aerodynamic loads¹⁻³. In addition, conventional aerodynamic control surfaces become ineffective in such situations because of vortex wakes generated by the forebody.

Both computational and experimental research showed that the vortices are very sensitive to small perturbations near the apex of a forebody⁴⁻⁶. Although methods have been developed to delay the onset of asymmetric vortex shedding, the fact that the separation vortices generate large airloads and are very sensitive to small perturbations offers an exceptional opportunity for manipulating them with little energy input to achieve active lateral control of the vehicle in place of conventional control surfaces. Methods toward such a goal, by using various deployable mechanical devices and suction and blowing mechanisms, have been studied and reviewed by Malcolm⁷ and Williams⁸. Most of these methods are based on steady methods in the sense that the control actuation is through a static or steady excitation.

The separation vortices exhibit a bistable mode of asymmetry, in which the vortices assume one of two mirror-imaged asymmetric configurations at high angles of attack^{4,6,9}. Such bistable behavior makes continuous proportional control difficult to achieve with a conventional steady type of actuation. Bernhardt and Williams¹⁰ used unsteady blowing near the forebody apex of an ogive-cylinder model and demonstrated the possibility of switching the flow from one of its asymmetric bistable modes to the other at 45° and 55° angle of attack. The proportional control has not achieved because the blowing was done either on the port or starboard side only.

Realizing that the flow may respond continuously to dynamic alternating excitations, Hanff et al.¹¹ alternated blowing from two forward facing nozzles near the apex of their test model to deliberately switch the vortices between their two bistable configurations with given duty cycles and at fast enough frequencies. Ming and Gu [12] used a miniature swinging strake mounted at the apex of their ogive cylinder model. They discovered that the flow would respond continuously to the mean angle settings if the frequency and amplitude of the oscillation of the strake are tuned appropriately. By using such ingenious unsteady dynamic controls, both groups succeeded in demonstrating the feasibility of proportional control on the side forces over slender ogive forebodies.

Plasma active flow control has received growing attention in recent years because of the advantages of not having mechanical parts, zero reaction time, broader frequency bandwidths and relatively low energy consumption. What is most important, the plasma actuators can be arranged conveniently on the parts surface of the vehicle. Many researchers choose the single dielectric barrier discharge (SDBD) as the plasma actuation type. The effect of the SDBD actuator is to impart momentum to the flow, much like flow suction or blowing but without the mass injection. Post and Corke^{13,14} successfully demonstrated their use in the control of separation over stationary and oscillating airfoils. Huang et al.¹⁵ also used them to control separation over turbine blades. A review is provided by Corke and Post¹⁶. Nelson et al.¹⁷ used a pair of plasma actuators which located at the $\pm 120^\circ$ from the leeward meridian near the nose of a tangent ogive nose/cylindrical model to manipulate the forebody vortices. The experiments have confirmed that the plasma actuator can be used to displace the vortex on the forebody model by the Coanda effect.

Recently, Liu et al.¹⁸ reported wind-tunnel experiments that demonstrate nearly linear proportional control of lateral forces and moments over a slender conical forebody at high angles of attack by employing a novel design of a pair of single dielectric barrier discharge (SDBD) plasma actuators near the cone apex combined with a duty cycle technique. Meng et al.¹⁹ showed the linearity of the controlled lateral forces and moments with respect to the duty cycle can be improved via improved design parameters of the actuators.

The purpose of a great deal of research discussed above is to increase aircraft control capability at large angles of attack. For the practical super-maneuverability of a modern aircraft at high angles of attack, the flight speed is demanded beyond $0.1M$ at least. That is to say, if an active flow control technology can be incorporated on a

production aircraft, one of the essential condition is that it is effective at higher wind speed. But the active flow control technique on the slender forebody discussed above are almost performed at very low wind speeds and Reynolds number, especially for plasma flow control technique (as listed in table 1, some test speeds are calculated with Reynolds number and characteristic dimension, where v is chosen as 14.9 million). The main objective of the following research is to increase the test velocity with effective plasma flow control via changing the position and the direction of the induced flow of the plasma actuator in comparison with the former research^{18,19}.

Table 1. Brief Introductions of Some Forebody Vortex Control Experiments

Researchers	Experimental technique	Angles of attack	Reynolds number	Test speed (m/s)
John E. Bernhardt and David R. Williams ¹⁰	Unsteady blowing	45°, 55°	6,300	3.3 (Calculated)
Ernest Hanff, Richard Lee and Richard J. Kind ¹¹	Unsteady blowing	0°-70°	176,000	40 (Presented)
Xiao Ming and Yunsong Gu ¹²	Swinging strake	55°	20,000	4.8 (Calculated)
Takashi Matsuno, Hiromitsu Kawazoe and Robert C. Nelson ¹⁷	Plasma actuation	45°	5,000	9.22 (Presented)
Feng Liu, Shijun Luo, Chao Gao, Xuanshi Meng et al. ¹⁸	Plasma actuation	30°-50°	5,000	5.0 (Presented)
Tzong-Shyng Leu, Jeng-Ren Chang, Pong-Jeu Lu ²¹	Flexible micro balloon actuators	50°, 55°	6,7000	20 (Presented)

II. Experimental Setup

A. Wind-Tunnel Facility

The flow-control experiments are performed in a 3.0m×1.6m open-circuit low-speed wind tunnel at Northwestern Polytechnical University. The cone-cylinder model is tested at $\alpha = 45^\circ$ and 50° . The free stream velocity $U_\infty = 15 \text{ m/s} \sim 30 \text{ m/s}$ with Reynolds numbers ranging from 0.16 to 0.32 million based on the cone base diameter.

B. Forebody Model configuration

Because the nose of any pointed forebody is locally conical in shape, the flow may be regarded as locally equivalent to that about a tangent cone. For this reason, an experimental model of a circular cone with a 10 degree semi-apex angle faired to a cylindrical afterbody is tested (As that used in Ref. [18, 19]). The model consists of two separate pieces. The frontal portion of the cone is made of plastic and has a length of 150 mm. The rest of the model is made of metal. The total length of the cone is 463.8 mm with a base diameter of 163.6 mm.

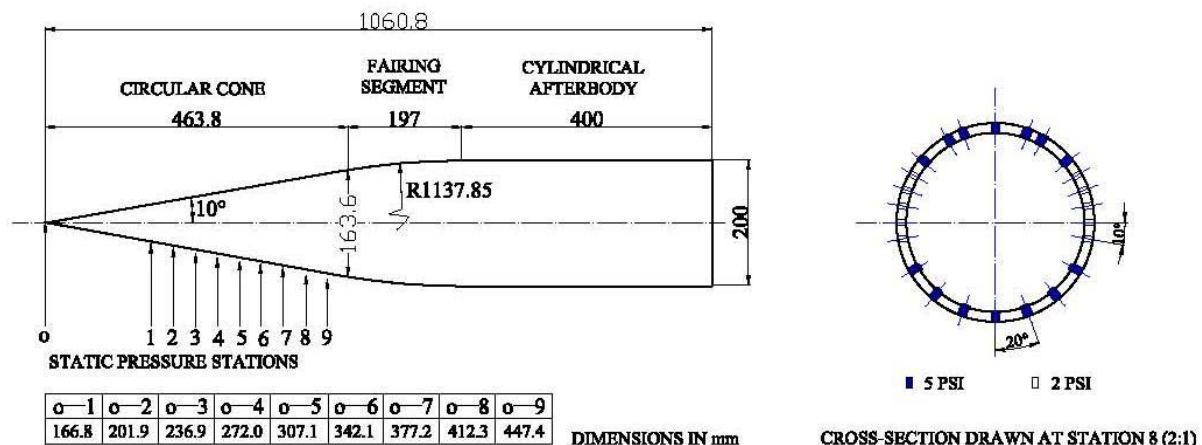


Figure 1. The model and unsteady pressure tapings arrangements sketch

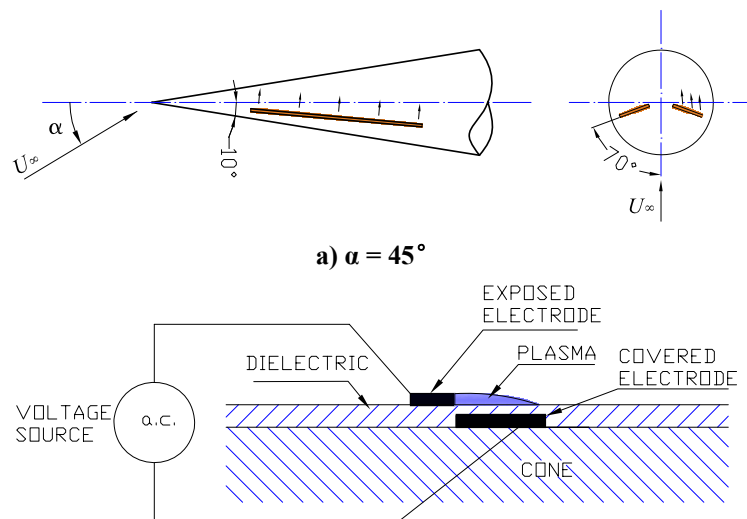
The time-averaged pressure tappings are arranged in 10° increments around the azimuth of the cone at 8 stations (left in figure 1), so there are totally 36×8 pressures taps used to detect changes in the configuration of the vortices. The model of pressure taps is 9816 by the PSI Company with an accuracy of up to $\pm 0.05\%$ FS, which are read at frequency of 100 Hz. The sectional and overall side force, and yawing moment are calculated from the measured pressures. The sectional side-force coefficient $C_{y,d}$ is normalized with the local diameter d and is positive when pointing to the starboard side of the cone. The yawing moment coefficient C_n is taken about the cone base and positive when yawing to the starboard side, and normalized with the base diameter D and base area S . The model is carefully cleaned prior to each run of the wind tunnel.

C. Design Concept of Single Dielectric Barrier Discharge Plasma Actuator

One pair of long strips of SDBD plasma-actuators are placed symmetrically on the plastic frontal cone near the apex as shown in Fig. 2(a). The plasma actuator consists of two asymmetric copper electrodes each of 0.03 mm thickness. A thin Kapton dielectric film wraps around the cone surface and separates the covered electrode from the exposed electrode as shown in Fig. 2(b). The length of the electrodes is 100 mm along the cone meridian with the leading edge located at 15 mm from the cone apex. The width of the exposed and covered electrode is 2 mm and 10 mm, respectively. There is no gap or overlap between the exposed and covered electrode.

The actuators are each connected to a high voltage ac source (model CTP-2000K by Nanjing Suman Co.) that provides about 13 kV peak-to-peak voltage sinusoidal excitation to the electrodes at a frequency of 8.5 kHz.

Three modes of operations of the actuators are defined. The plasma-off mode corresponds to the case when neither of the two actuators is activated. The plasma-on mode refers to the conditions when either the port or starboard actuator is activated while the other is kept off during the test. These are called the port-on and starboard on modes, respectively. The third mode employs a duty-cycle technique in which the two actuators on the cone is activated alternately with a specified duty cycle, τ , defined as the fraction of time when the starboard actuator is on over a duty-cycle period. The fraction of time that the port actuator is on is then $1 - \tau$. The duty cycles are achieved by modulating the carrier AC voltage sources by a digital pulse wave generator. The optimum unsteady actuator frequency f can be found such that $f^+ = 1^{20}$. Comply with this rule, the duty-cycle frequency can be found at various free-stream velocity, which is 75 Hz, 150 Hz for 15 m/s, 30 m/s wind tunnel speed, respectively.



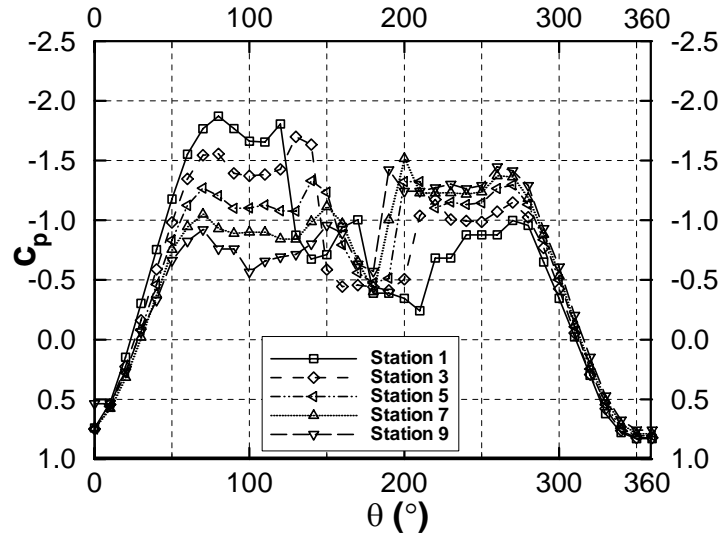
b) Single Dielectric Barrier Discharge
Figure 2. Sketches of the plasma actuators.

It should be pointed out that the design parameter is referred to the reference¹⁷, but we make some changes. The right edge of the exposed electrode shown in Fig. 2 b) is aligned with the cone at the azimuth angle $\theta = \pm 70^\circ$ ($\theta = \pm 60^\circ$ in Reference¹⁷) which are nearer to the separation lines, where θ is measured from the windward meridian of the cone and positive is clockwise when looking upstream (Fig. 2 a)). The direction of the induced flow produced by actuators is downstream. The design idea for the position and the induced flow direction is intended to affect the boundary-layer separation positions via a plasma-induced Coanda effect. The actuators are hand-made and attached directly to the cone surface with no allowance.

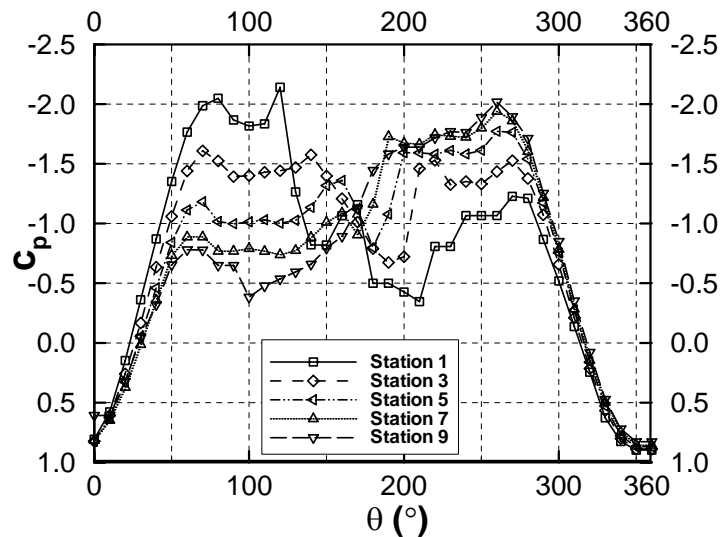
III. Experimental Results and discussion

A. Base plasma-off flow

To check the flowfield states for plasma off, Figures 3 presents the time-averaged pressure distributions on odd-numbered measured stations at $\alpha = 45^\circ$ and 50° , $U_\infty = 15$ m/s. The sectional pressure distributions indicate the flow is essentially asymmetric around the cone.



a) $\alpha = 45^\circ$



b) $\alpha = 50^\circ$

Figure 3. Time-averaged pressure distributions over odd-numbered stations at $U_\infty = 15$ m/s, Plasma off.

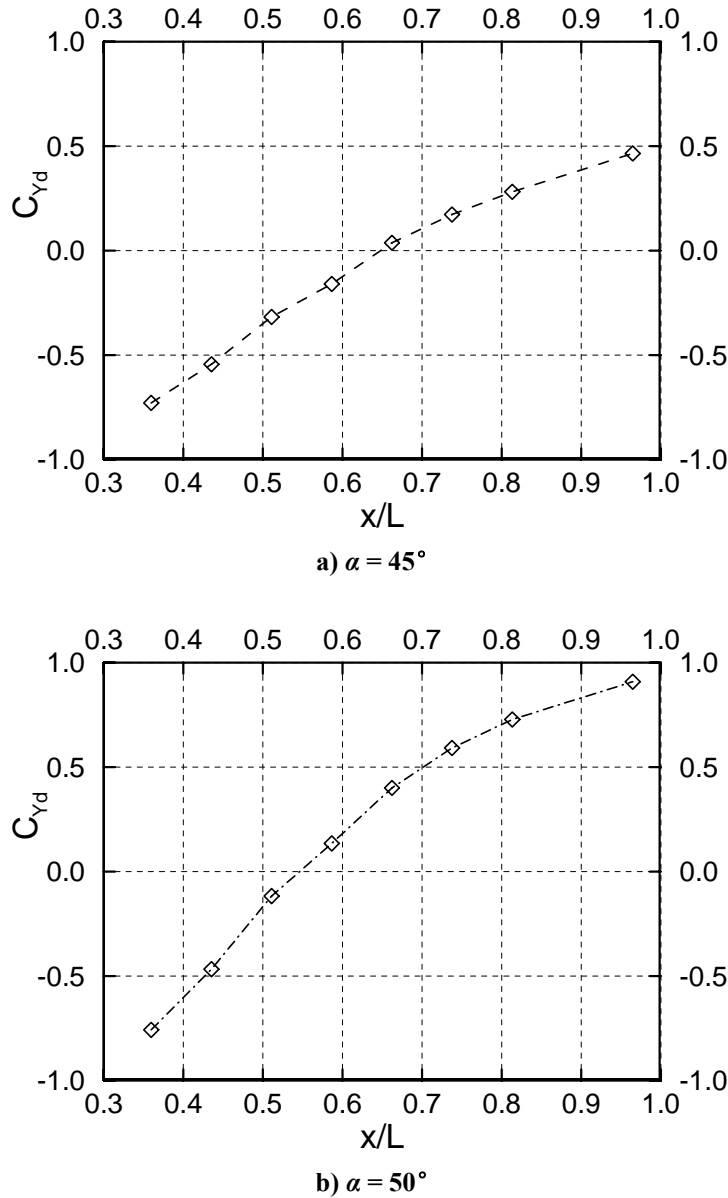


Figure 4. Time-averaged local-side force coefficient versus x/L at $U_\infty = 15$ m/s, Plasma off.

The local force distributions along the cone axis are calculated from the measured pressure data. Figure 4 present time-averaged local-side force C_{Yd} versus x/L . It appears that C_{Yd} would approach a non-zero limit when the variable x approaches zero. Since C_{Yd} is normalized by the local diameter d , the sectional side force is proportional to d as the section approaches the body apex. Therefore, the pressure asymmetry does occur right at the apex of the body. This was observed in smoke visualization using a high-magnification lens by Zilliac et al. [4]. At $\alpha = 50^\circ$, the C_{Yd} is also changing with x/L , but the curve becomes much more nonlinear and the position where the signal from positive to negative is moved up from about $x/L = 0.65$ to $x/L = 0.55$.

As we see, the pressure distribution changes along the measured stations. Accordingly, C_{Yd} is changing near linearly and from positive to negative, or vice versa between neighboring pressure stations. So we may refer that there are more than two vortices appearance along the cone segment. Tzong-Shyng Leu et al.²¹ used the micro balloon actuators on a cone-cylinder slender body. The measurements results of X-type hot wire clearly indicate that a third vorticity-concentrated area is clearly found in the weak vortex side before and after the actuation. The appearance of the third vortices make the flowfield over conical cone at $\alpha = 45^\circ$ and 50° with 0.16 million Reynolds

number be not bistable. But it is seen from the pressure distributions that no vortex breakdown occurs over the cone forebody.

B. Pressures, Lateral Forces and Moments with Plasma Control

Figure 5 presents the time averaged pressure distributions on odd-numbered Stations at $\alpha = 45^\circ$, $U_\infty = 15$ m/s for various cases, $\tau = 0.01-0.99$ denote plasma duty cycles. At measured station 1, when port plasma occupied the almost work time ($\tau = 0.01$), the higher suction peak appears on the port side of the cone, the pressure distributions are similar to that for plasma off. For various duty cycles ($\tau = 0.01-0.99$), the higher suction peak changes continuously from port side to starboard side. The pressure distributions for τ , and $1 - \tau$ are not likely anti-symmetric, which may happen when the flowfield is bistable. At measured station 3, the pressure distributions for τ , and $1 - \tau$ are most likely symmetric, but not strictly. From station 5 to the rear measured stations, at $\tau = 0.01$, the higher suction peak appears on the starboard side of the cone, and it grows much higher continuously for various duty cycles.

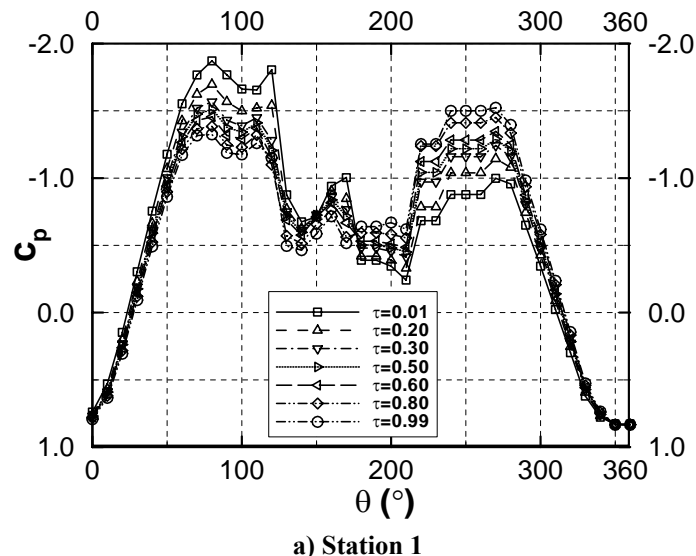
Figure 6 present time-averaged local side force C_{Yd} versus τ at $\alpha = 45^\circ$, it shows that proportional control of asymmetric force is achieved by the duty-cycled plasma actuations.

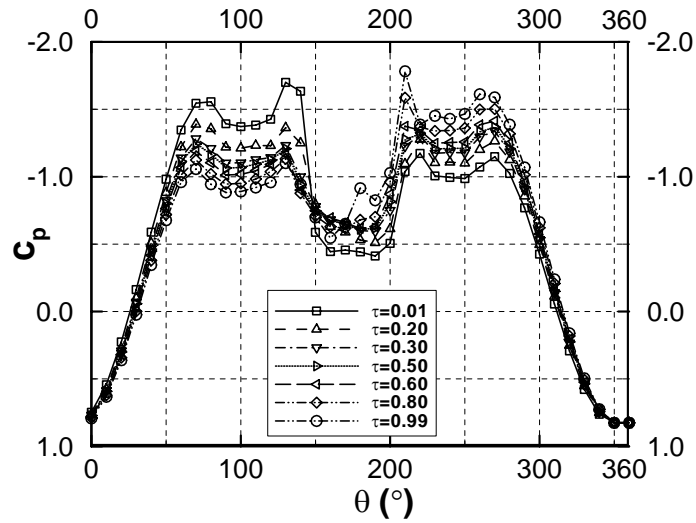
Figure 7 gives the overall side force coefficient C_Y and yawing moment coefficient C_n versus duty cycle $\alpha = 45^\circ$. The linearity of the side force and yawing moment with respect to the duty cycle is improved over previous studies due to the improved design of the actuators.

Figure 8 presents the time averaged pressure distributions on odd-numbered Stations at $\alpha = 50^\circ$, $U_\infty = 15$ m/s for various cases, At measured station 1, when $\tau = 0.01$, the higher suction peak appears on the port side of the cone, the pressure distributions is similar to that for plasma off. For various duty cycles ($\tau = 0.01-0.99$), the higher suction peak change continuously from port side to starboard side. The pressure distributions for τ , and $1 - \tau$ are not likely anti-symmetric. At measured station 3, when $\tau = 0.01$, the pressure distribution is nearly symmetric. The suction peak occurs on starboard side and grows much higher continuously for various duty cycles. From station 5 to the rear measured stations, the higher suction peak appears on the starboard side of the cone, and it grows much higher continuously for various duty cycles. But the variation range is smaller than that at $\alpha = 45^\circ$.

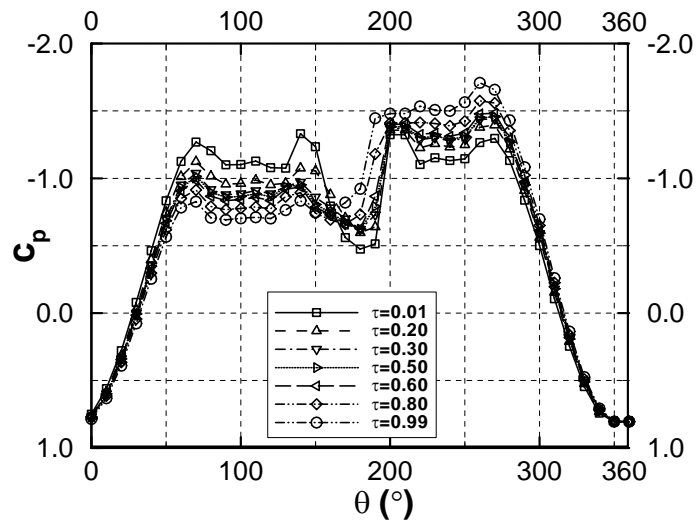
Figure 9 present time-averaged local side force C_{Yd} versus τ at $\alpha = 50^\circ$. it shows that proportional control of asymmetric force is achieved by the duty-cycled plasma actuations. Figure 10 gives the overall side force coefficient C_Y and yawing moment coefficient C_n versus duty cycle $\alpha = 50^\circ$. The linearity of the side force and yawing moment with respect to the duty cycle is not so good as that at $\alpha = 45^\circ$.

From time averaged pressure distributions changed with duty cycle ratios, we may find that the variation pattern of pressure distributions with plasma control under duty cycle model is determined at the measured station 1 which is closest to the plasma control region. For example, when $\alpha = 45^\circ$, $U_\infty = 15$ m/s, the higher suction peak turns down at port side and the pressure magnitude of starboard side is increasing continuously for various duty cycles. This rule is worked for the rear measured stations no matter what the original (for plasma off) sectional pressure distribution is.

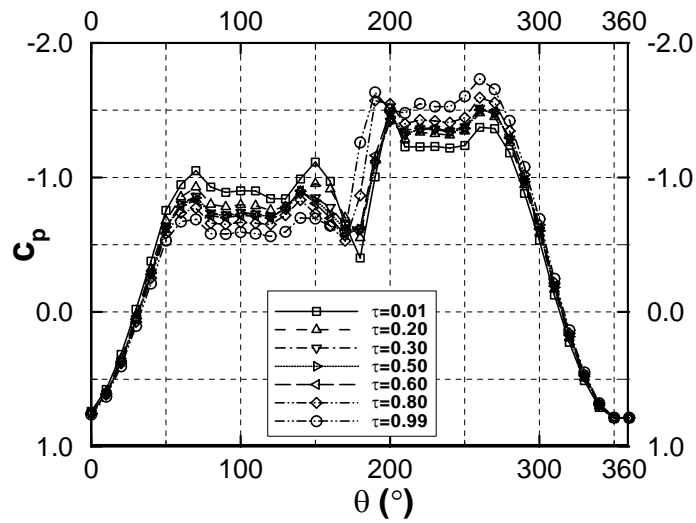




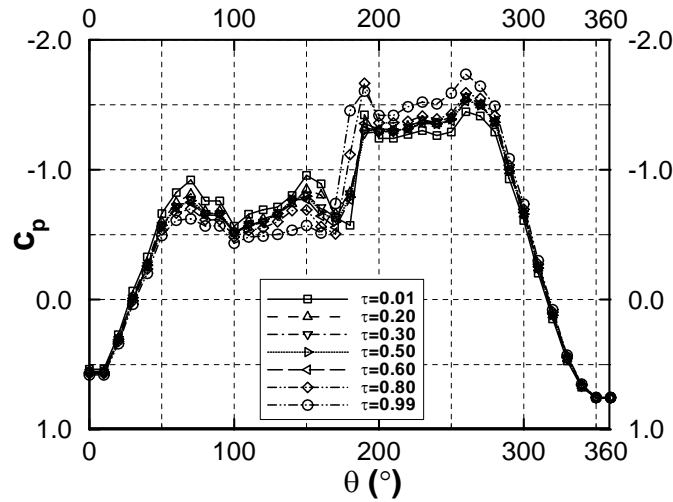
b) Station 3



c) Station 5



d) Station 7



e) Station 9

Figure 5. Comparison of time-averaged pressures for various duty cycles, odd Stations, $\alpha = 45^\circ$, $U_\infty = 15$

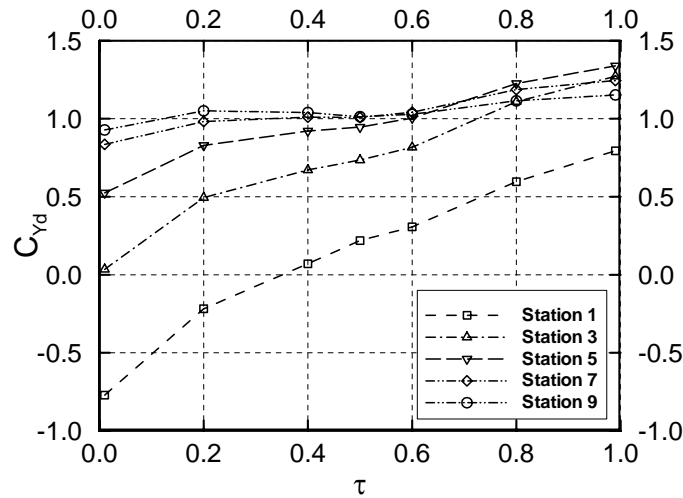
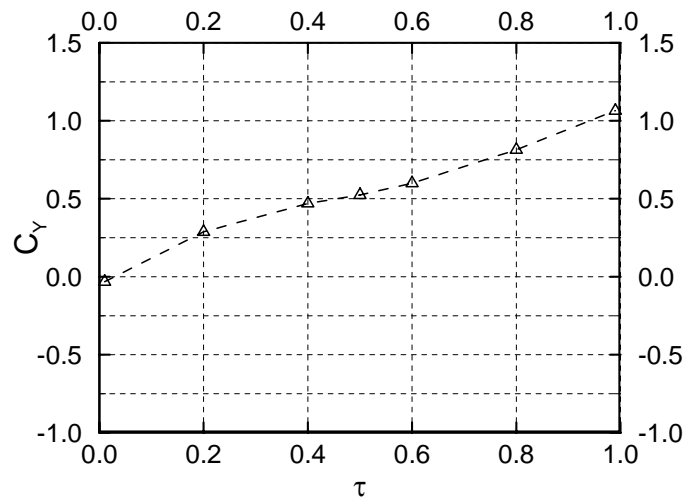
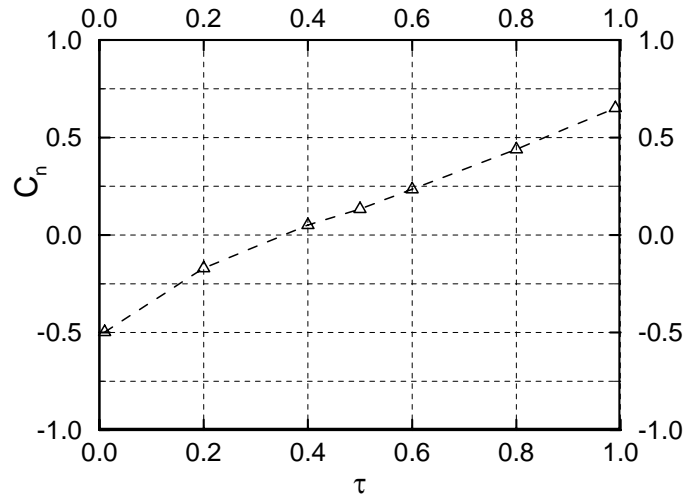


Figure 6. Time-averaged local side force vs. duty cycle, $\alpha = 45^\circ$, $U_\infty = 15$ m/s.

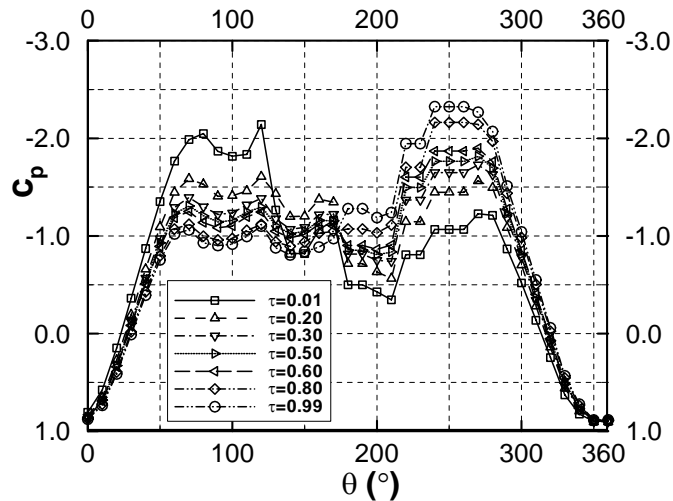


a) Side force coefficient

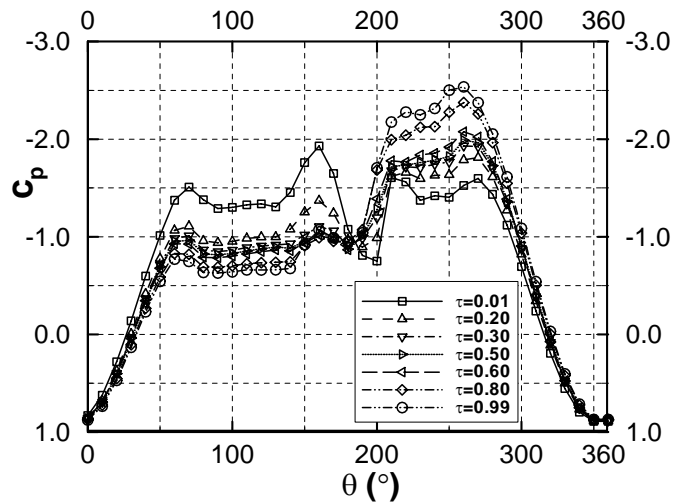


b) yawing moment coefficient

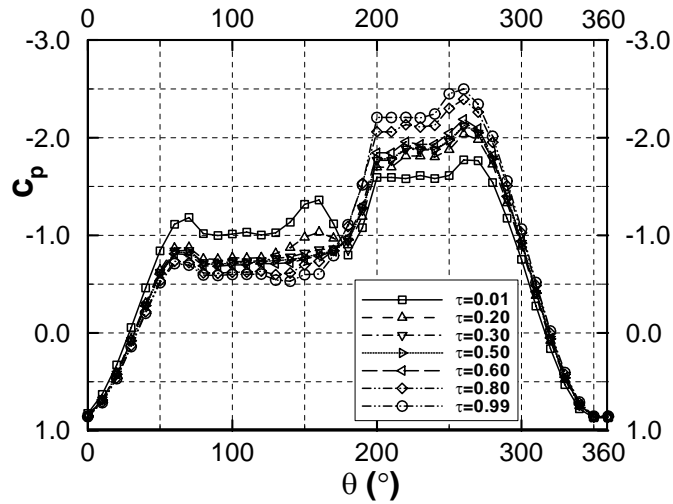
Figure 7. Time-averaged overall side force and yawing moment vs. duty cycle, $\alpha = 45^\circ$, $U_\infty = 15$ m/s.



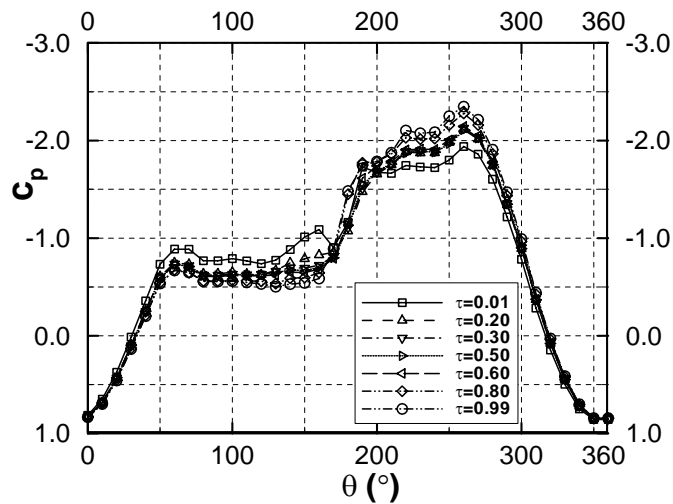
a) Station 1



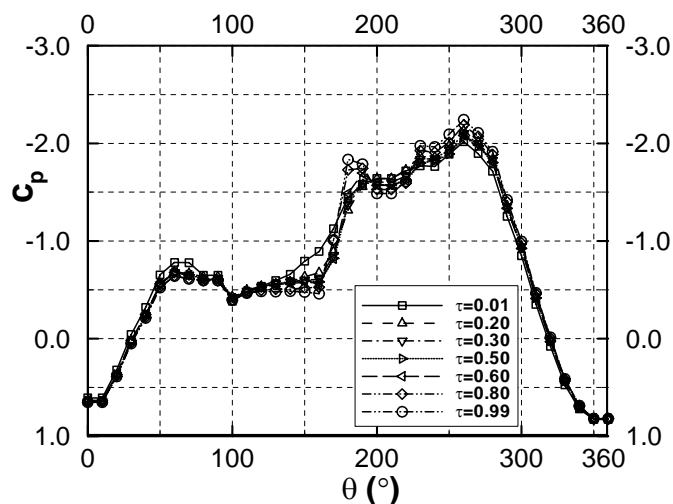
b) Station 3



c) Station 5



d) Station 7



e) Station 9

Figure 8. Comparison of time-averaged pressures for various duty cycles, odd Stations, $\alpha = 50^\circ$, $U_\infty = 15$ m/s.

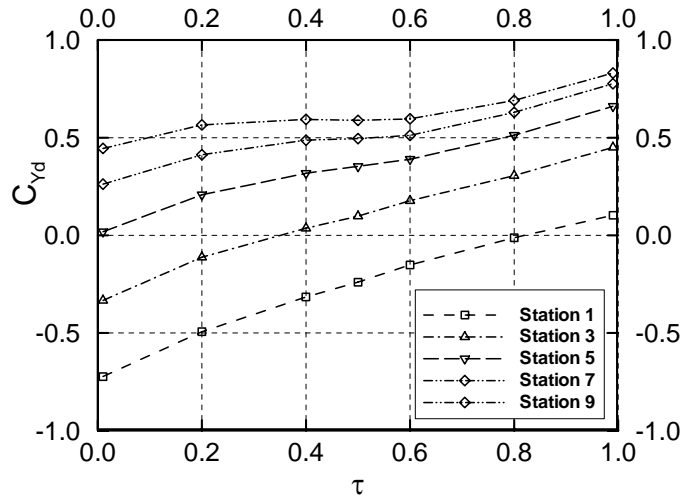
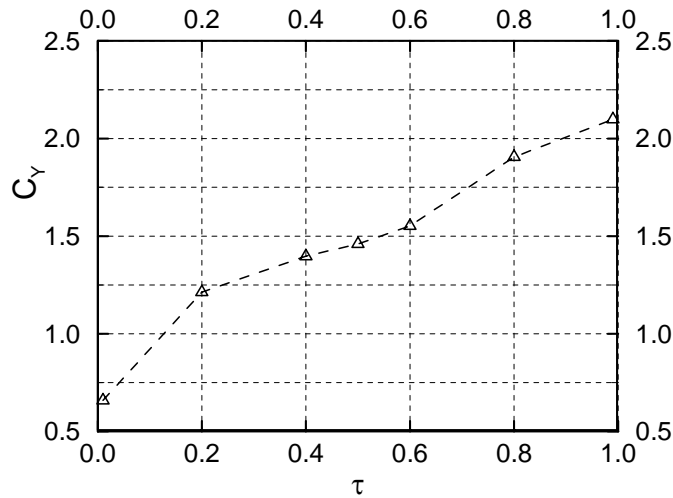
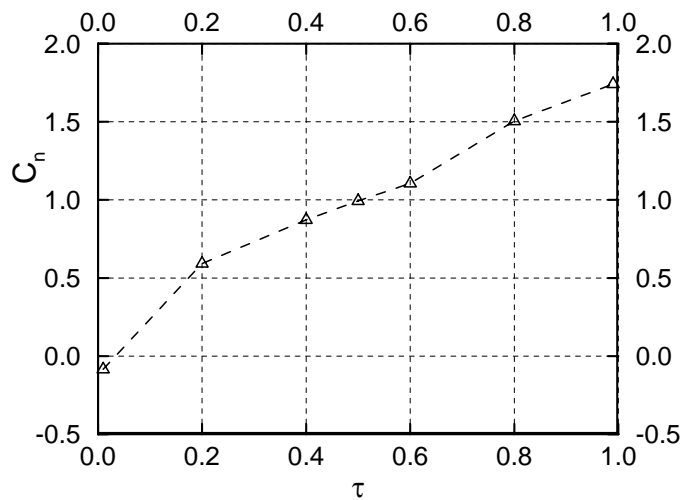


Figure 9. time-averaged local side force vs. duty cycle, $\alpha = 50^\circ$, $U_\infty = 15$ m/s.



a) Side force coefficient



b) yawing moment coefficient

Figure 10. Ensemble-averaged overall side force and yawing moment vs. duty cycle, $\alpha = 50^\circ$, $U_\infty = 15$ m/s.

C. Plasma Control with Higher Wind Speed

Experiments were performed for the plasma-off, starboard-on, and port-on modes at 30 m/s. The surface pressure distribution at station 1 with three control modes is shown in Figure 11 for $\alpha = 45^\circ$. The port-on results is almost overlap with those of the plasma-off result. Activating the starboard plasma actuator produces a clearly increase of the suction peak. The time-averaged local side force C_{Yd} versus x/L versus presents in figure 12 shown again that the variation pattern of pressure distributions with plasma control is determined at the plasma control region and then develops downstream.

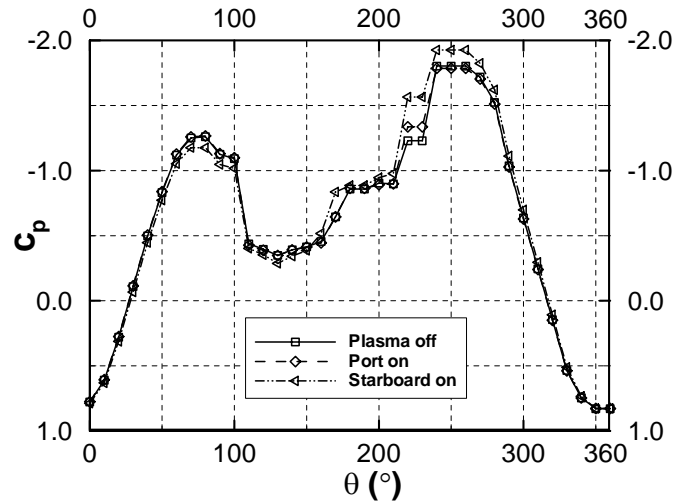


Figure 11. Comparison of pressure distributions for the plasma-off and -on conditions at $\alpha = 45^\circ$, $U_\infty = 30$ m/s.

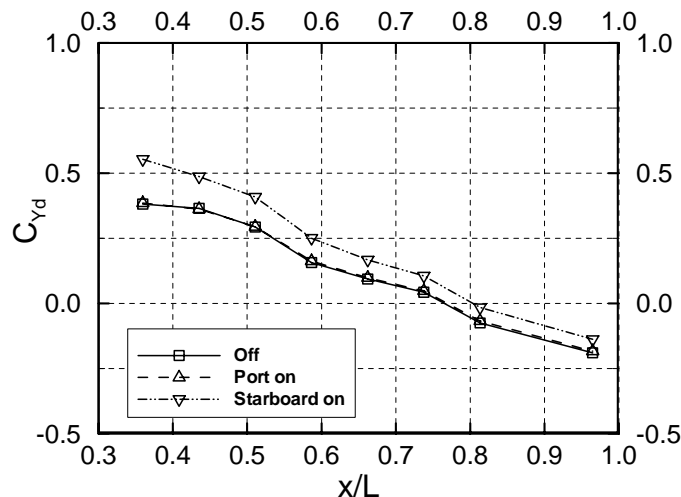


Figure 12. Local side force distributions under plasma-off and -on conditions.

IV. Conclusions

An active flow control by using plasma actuation is performed in a low speed wind tunnel. The results of the present paper reconfirm previous findings that it is possible to achieve linear proportional control of the lateral forces and moments of a slender circular-cone body by the duty-cycled plasma flow control technique with appropriately designed plasma actuators and selected electric parameters. An effective control with a relative higher wind speed is gotten by adjusting the position and induced flow direction of the plasma actuators. The results is discussed through analyzing the pressure data obtained by time-averaged pressure tappings. By using the present actuator design parameters, the magnitude of port pressure turns down and that of the starboard side is increasing continuously for various duty cycle ratios no matter what the original (for plasma off) sectional pressure distribution

is. It shows that the variation pattern of pressure distributions with plasma control is determined at the plasma control region and then develops downstream.

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